

EECS 245, Spring 2026

LEC 1

Introduction, Models,  
and Loss Functions

→ Read: Ch. 1 of notes


→ Course website: [eecs245.org](http://eecs245.org)

# Agenda

- Introductions
- What is machine learning, and what will we learn in this class? ← Ch. 1.1
- Logistics
- Models and loss functions ← Ch. 1.2-1.3
- Finding optimal parameters

Who am I?

\* Call me Suraj "soo-rudge"

- Just finished 2<sup>nd</sup> year as faculty @ Michigan
- Taught data science at UC San Diego 2021-24
- BS and MS in EECS from UC Berkeley
- From Windsor, ON 
- No TAs this spring - just me



Machine learning: automatically

learning patterns from data

# Taxonomy of machine learning



Labeled data

*not prediction: rather, finding structure*

Unlabeled data

Reward

Supervised learning

Unsupervised learning

Reinforcement learning

Quantitative prediction

Categorical prediction

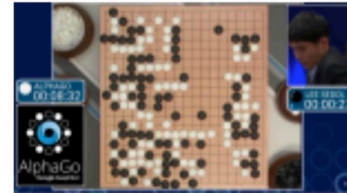
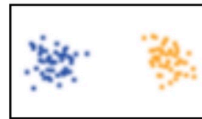
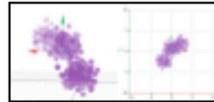
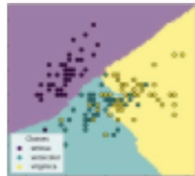
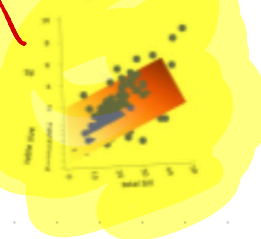
*predicting category*

Regression

Classification

Dimensionality reduction

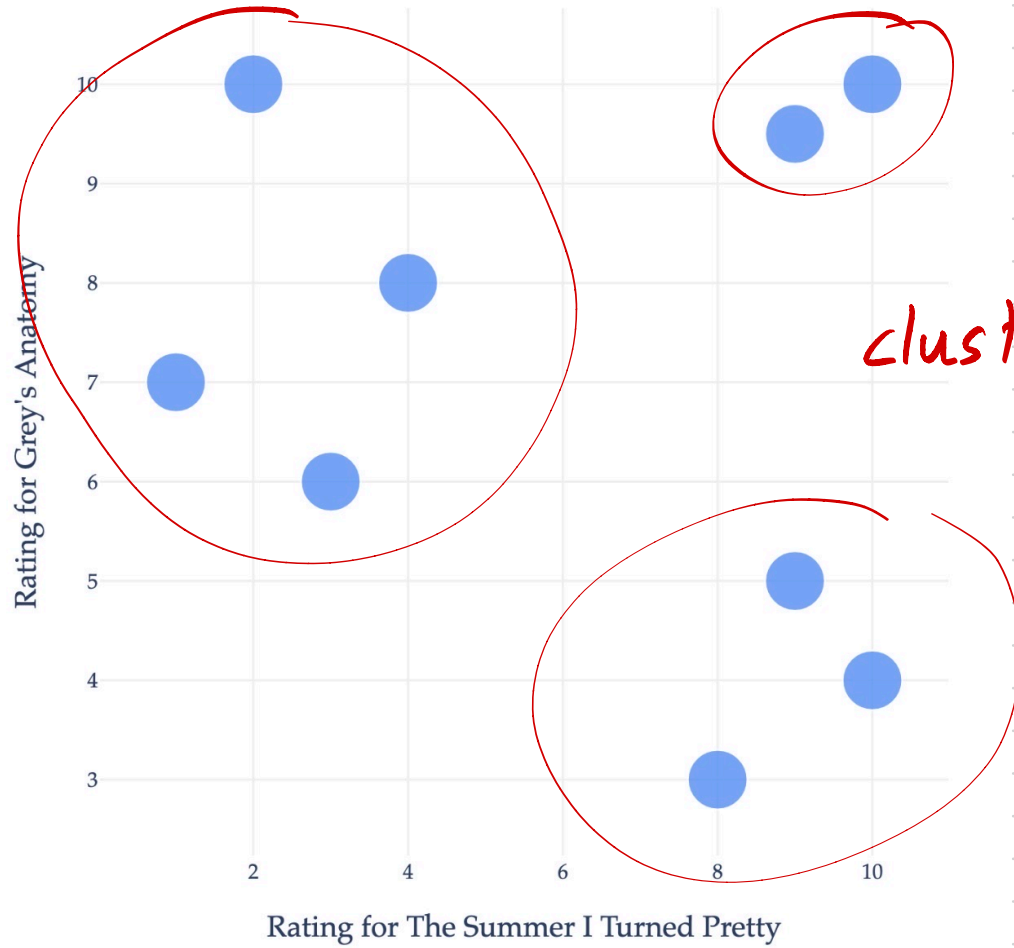
Clustering



AlphaGo

*predict given  $x$   $y$*

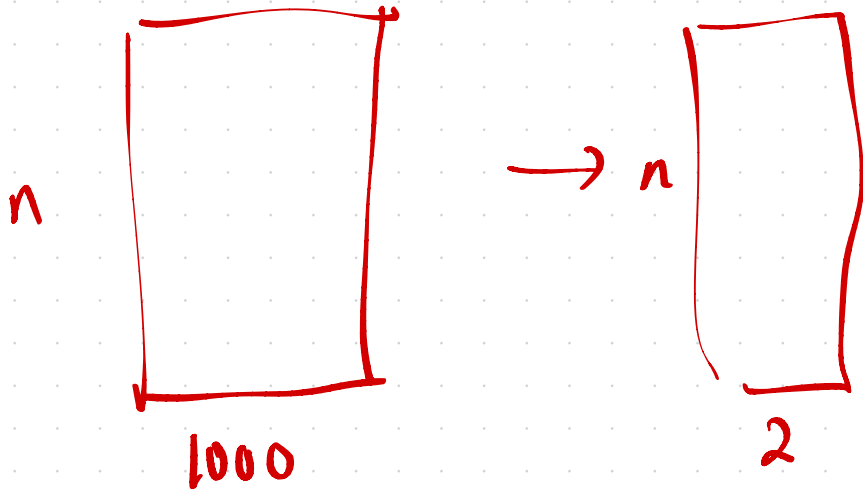
*predicting real number*



clustering

another example of unsupervised learning:

dimensionality reduction



1. Introduction to Supervised Learning
2. Simple Linear Regression
3. Vectors
4. Linear Independence
5. Matrices
6. Linear Transformations and Projections
7. Regression using Linear Algebra
8. Gradients
9. Eigenvalues and Eigenvectors
10. Singular Value Decomposition

Math for ML

Midterm 1

Midterm 2

post-Midterm 2

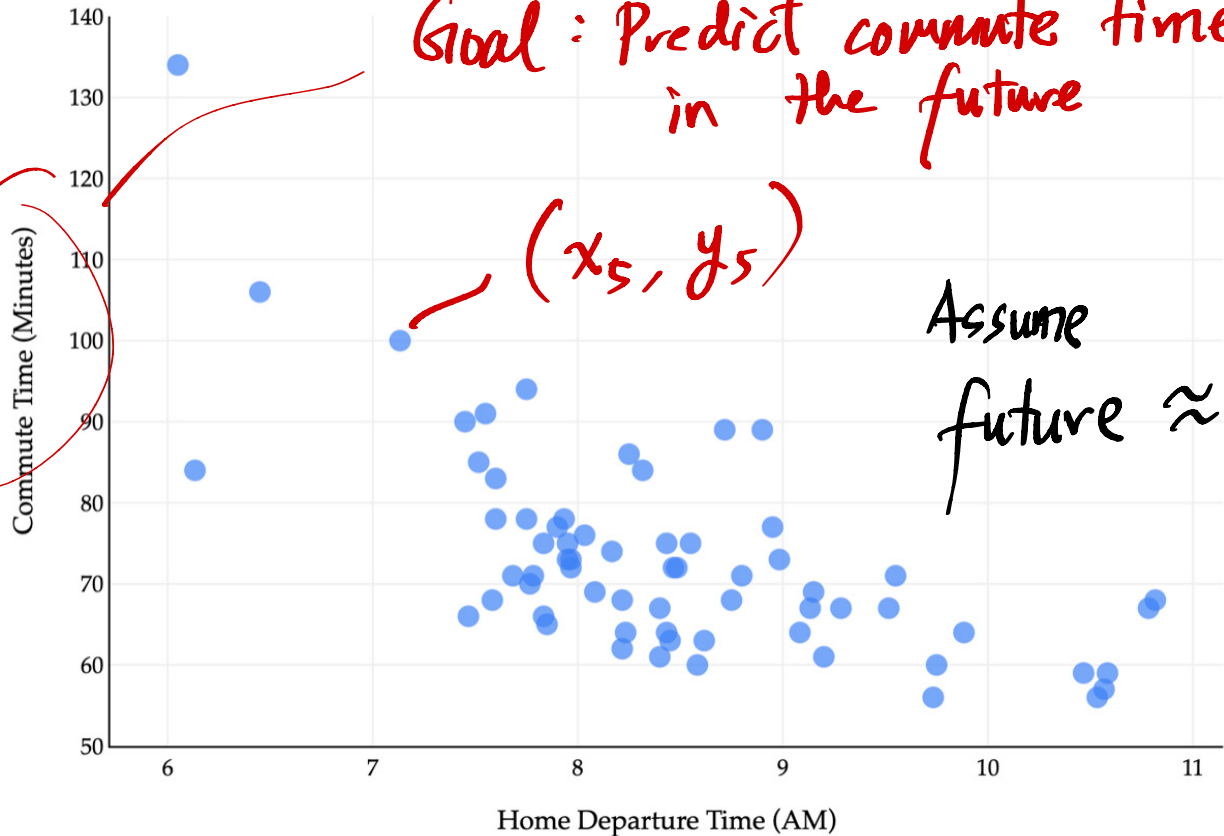
eeCS 245.org

starting Ch. 1.2 →

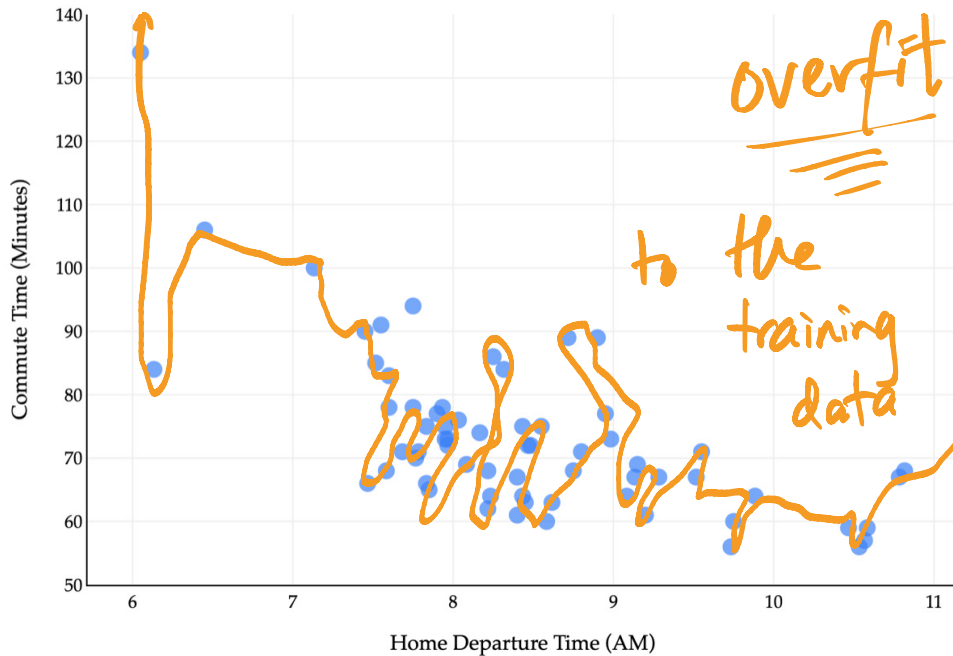
	date	day	departure_hour	minutes	label / target / output
0	5/15/2023	Mon	10.816667	68.0	
1	5/16/2023	Tue	7.750000	94.0	Commute time
2	5/22/2023	Mon	8.450000	63.0	
3	5/23/2023	Tue	7.133333	100.0	
4	5/30/2023	Tue	9.150000	69.0	

Goal: given an  $x_i$   
predict  $y_i$

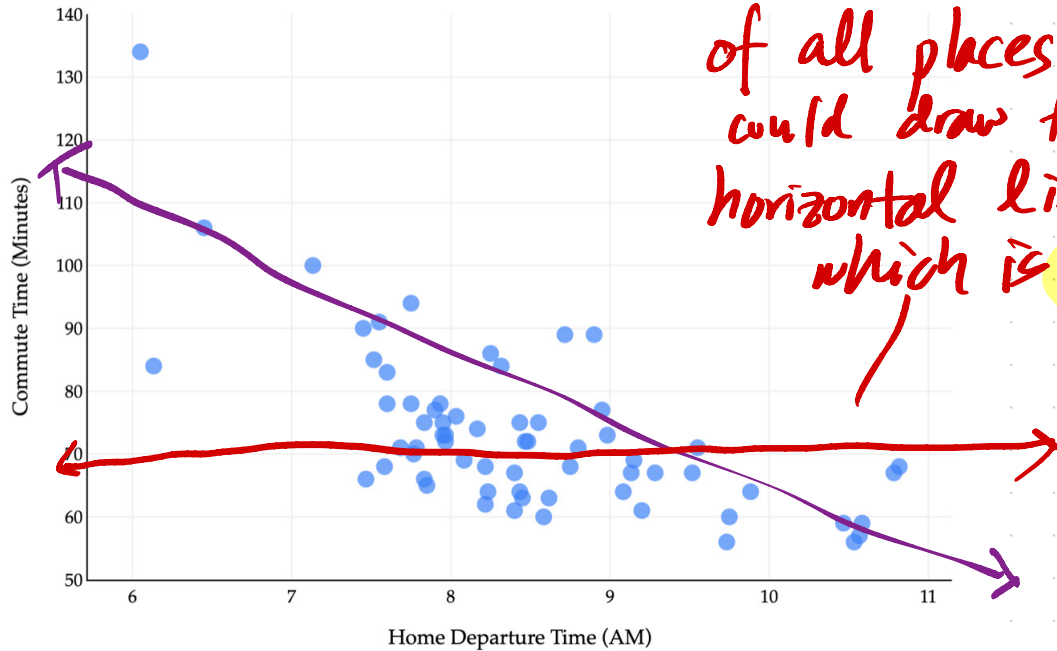
8 am + 45% of an hour  
= 8:27am



Model : A set of assumptions about how data was generated



bad:  
we want to generalize to unseen data.



of all places I could draw this horizontal line which is best?

① constant model

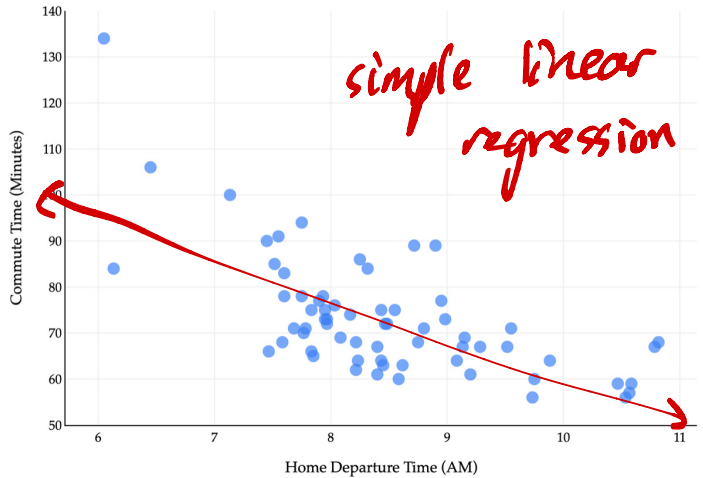
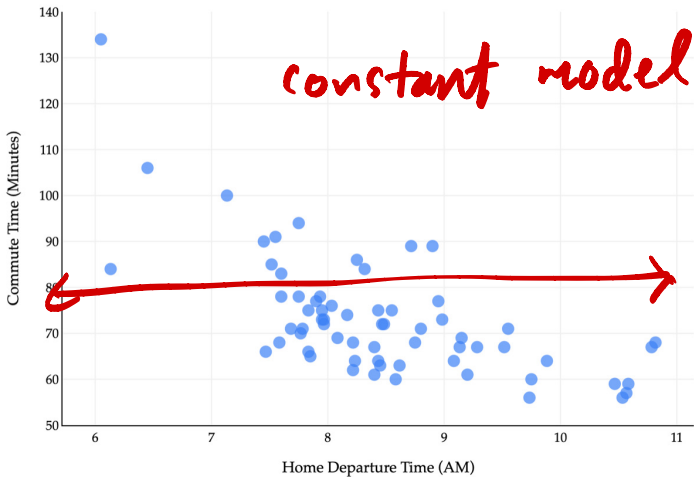
② simple linear regression  
line of best fit

Hypothesis function,  $h$ , takes in features and returns predictions (predicted  $y$ -values)

departure hour  $x_i$

$$h(x_i) = 80$$

$$h(x_i) = 100 - 4x_i$$



Parameters,  $w$

Q: How do you find the "best" parameters?

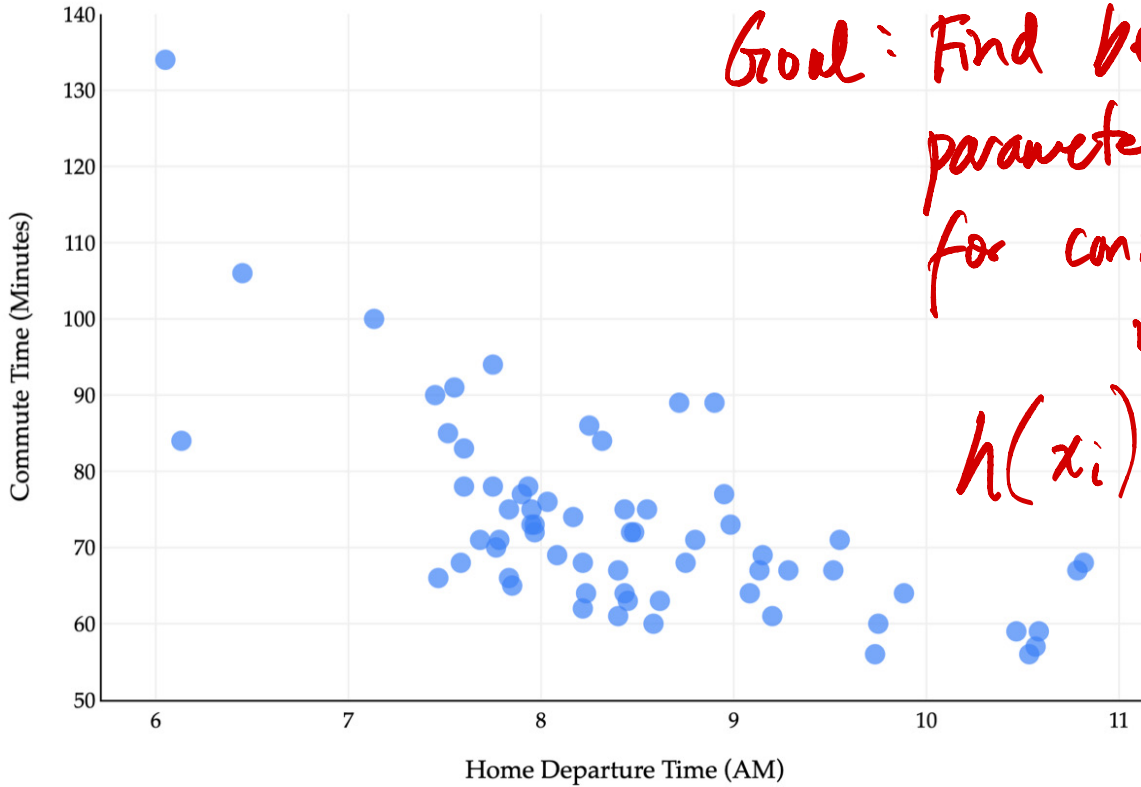
- Constant model: one parameter

$$h(x_i) = w$$

- Simple linear regression model: 2 parameters

$$h(x_i) = w_0 + w_1 x_i$$

↑ slope            ↑ intercept



# Error

$$e_i = \underbrace{y_i}_{\text{actual}} - \underbrace{h(x_i)}_{\text{predicted}}$$

for constant model,  
this is just  
 $h(x_i) = w$

e.g.  $y_i = 80$

① if  $h(x_i) = 75 \rightarrow \text{error} = 5$

② if  $h(x_i) = 72 \rightarrow \text{error} = 8$

③ if  $h(x_i) = 100 \rightarrow \text{error} = 80 - 100 = -20$

Loss function : describes the quality of a prediction for a single data point

① Squared loss :

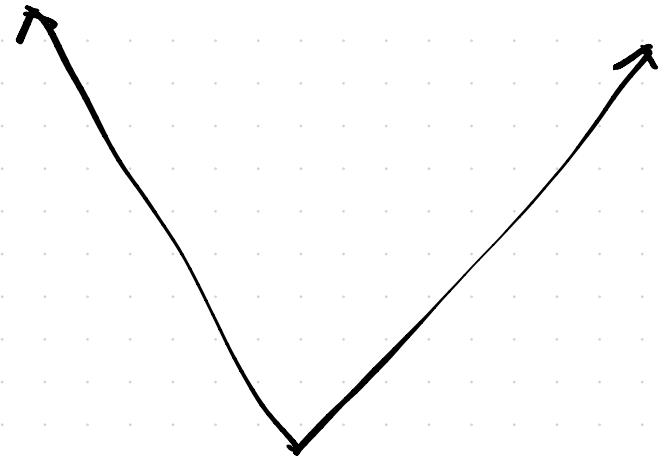
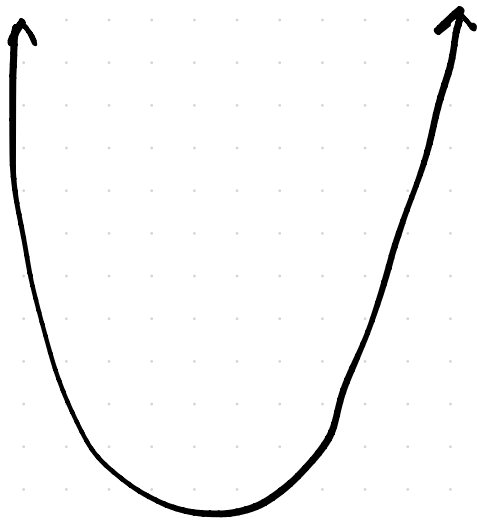
$$L_{sq}(y_i, h(x_i)) = (y_i - h(x_i))^2$$

(actual - predicted)<sup>2</sup>

default choice

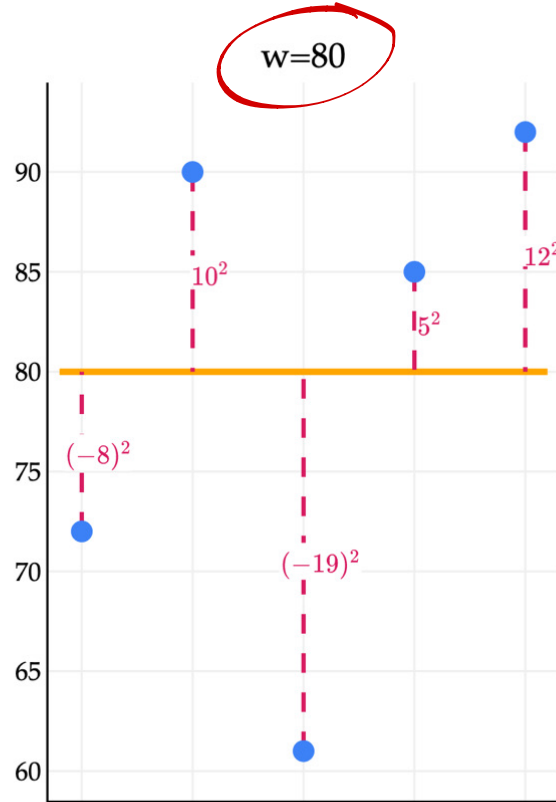
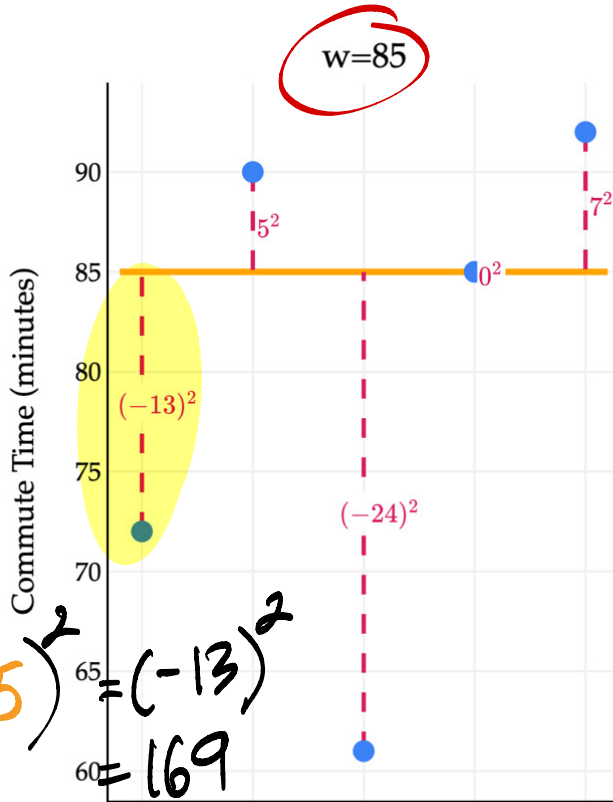
② Absolute loss :

$$L_{abs}(y_i, h(x_i)) = |y_i - h(x_i)|$$



not  
differentiable!

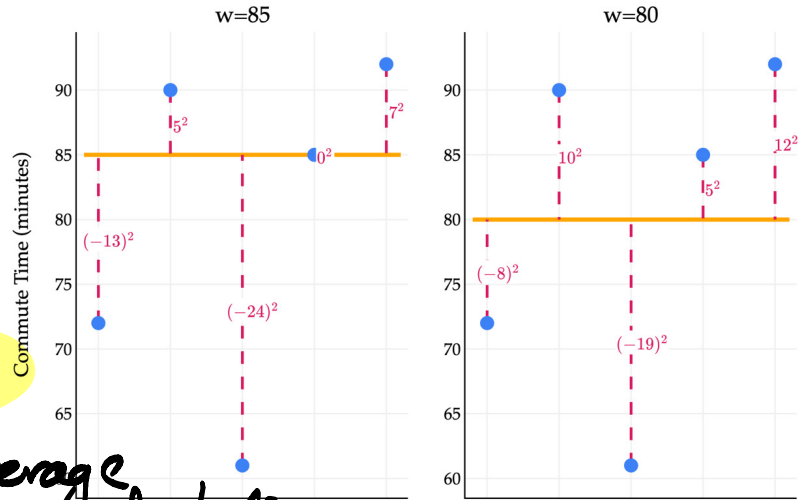
72, 90, 61, 85, 92  
 $y_1$   $y_2$   $y_3$   $y_4$   $y_5$



Average squared loss gives one number that describes the quality of a parameter across the whole dataset

•  $w = 85: \frac{(-13)^2 + 5^2 + (-24)^2 + 0^2 + 7^2}{5} = 163.8$

•  $w = 80 = \frac{(-8)^2 + 10^2 + (-19)^2 + 5^2 + 12^2}{5} = 138.8$



80 better than 85: lower average squared loss

72, 90, 61, 85, 92  
 $y_1$   $y_2$   $y_3$   $y_4$   $y_5$

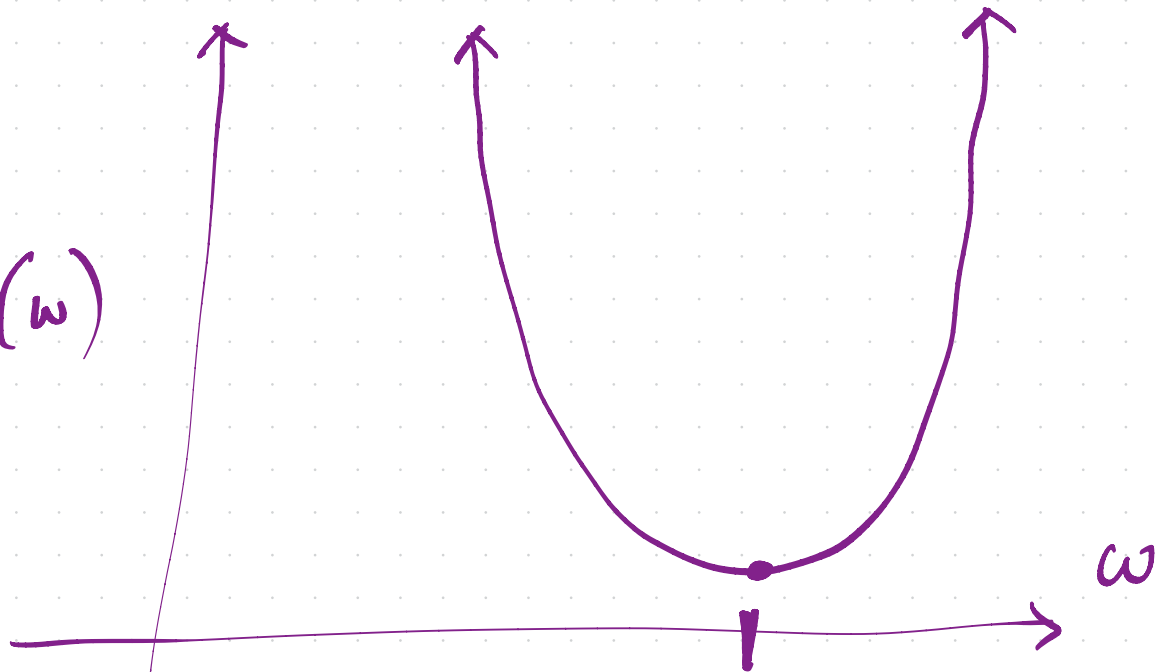
$$R_{sq}(w) = \frac{(72-w)^2 + (90-w)^2 + \dots + (92-w)^2}{5}$$

$L$ : loss for a single data point

$R$ : average loss across whole dataset

empirical risk

$R_{sq}(\omega)$



???????

Given  $y_1, y_2, \dots, y_n$  (all numbers)

Goal: Find the best constant prediction,  $w$

How? By minimizing average squared loss:

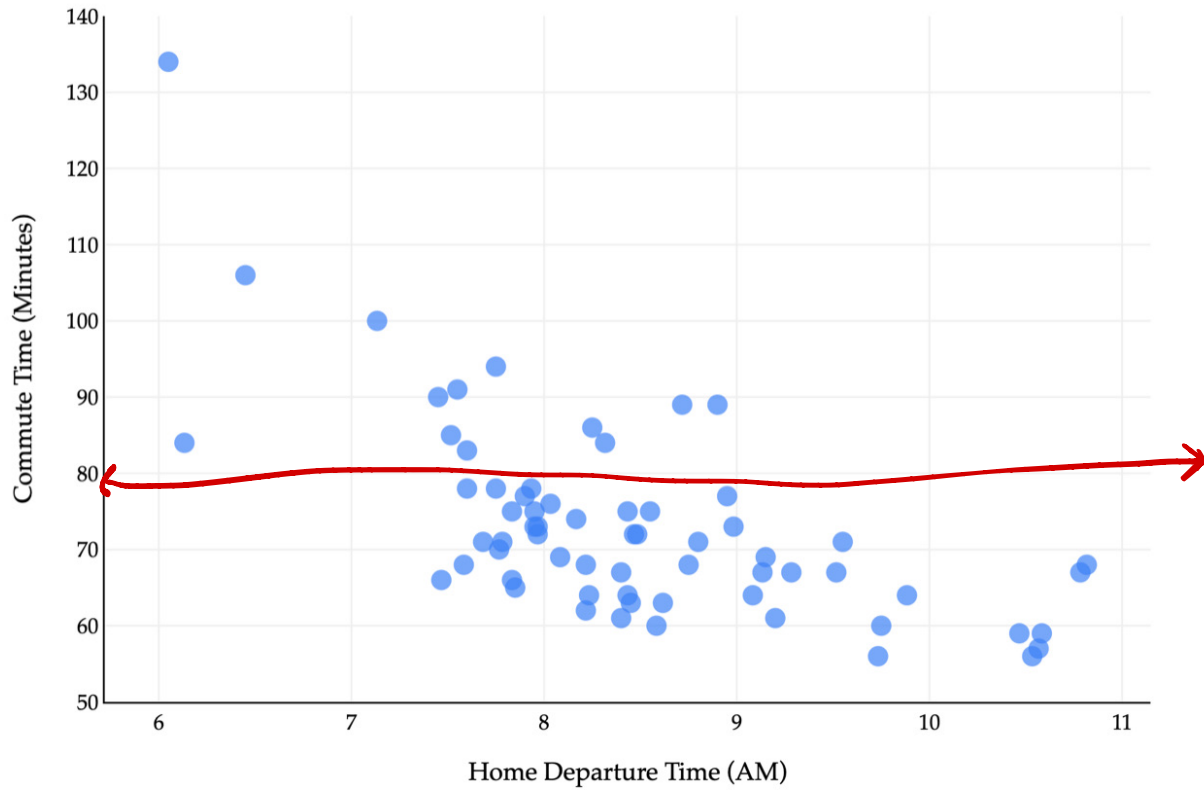
$$R_{sq}(w) = \frac{(y_1 - w)^2 + (y_2 - w)^2 + \dots + (y_n - w)^2}{n}$$

$$= \sum_{i=1}^n \frac{(y_i - w)^2}{n} = \frac{1}{n} \sum_{i=1}^n (y_i - w)^2$$

need to minimize!

Terminology:

"average squared loss" = "mean squared error"



Minimize

$$R_{sq}(w) = \frac{1}{n} \sum_{i=1}^n (y_i - w)^2$$

function of  $w$  only!

How to minimize function of one variable?

① Take derivative with respect to  $w$

② Set equal to 0

③ Verify we found a minimum (rather than a maximum)

$$R_{sq}(w) = \frac{1}{n} \sum_{i=1}^n (y_i - w)^2$$

$$\frac{dR}{dw} = \frac{1}{n} \sum_{i=1}^n \frac{d}{dw} (y_i - w)^2$$

$$= \frac{1}{n} \sum_{i=1}^n (-2) (y_i - w)$$

$$= -\frac{2}{n} \sum_{i=1}^n (y_i - w)$$

$a(x) + b(x) + c(x) + \dots$

derivative:  $\frac{da}{dx} + \frac{db}{dx} + \frac{dc}{dx}$

Aside :

$$\frac{d}{dw} (y_i - w)^2 = \underbrace{2 (y_i - w)}_{\text{power rule}} \underbrace{\frac{d}{dw} (y_i - w)}_{\text{chain rule}}$$

$$= 2 (y_i - w) (-1)$$

$$= -2 (y_i - w)$$

$$\frac{dR}{dw} = -\frac{2}{n} \sum_{i=1}^n (y_i - w)$$

set equal to 0 and solve for  $w$

$$-\frac{2}{n} \sum_{i=1}^n (y_i - w) = 0$$

sum of errors is 0!

$$\sum_{i=1}^n (y_i - w) = 0$$

$$\sum_{i=1}^n y_i - \underbrace{\sum_{i=1}^n w}_{w+w+\dots+w = nw} = 0 \Rightarrow$$

$$\frac{\sum_{i=1}^n y_i}{n} = w^*$$

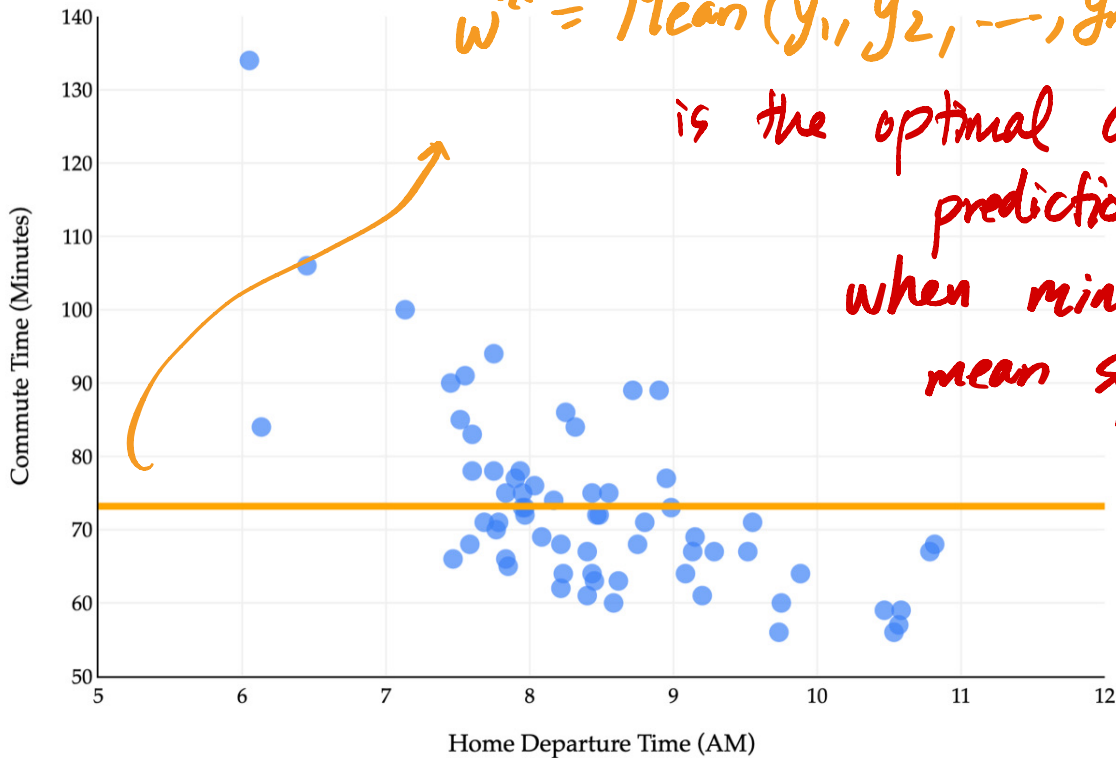
Mean of  $y_i$ 's  
is the  
best constant  
prediction!

$w^*$  : optimal parameter

(best)

$$w^* = \text{Mean}(y_1, y_2, \dots, y_n) = \bar{y}$$

is the optimal constant prediction, when minimizing mean squared error



# "Three-step modeling recipe" for making good predictions

① Choose a model

$$h(x_i) = w \quad \text{"constant model"}$$

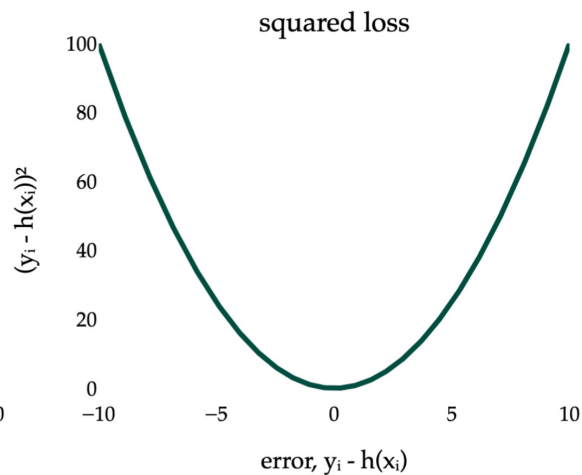
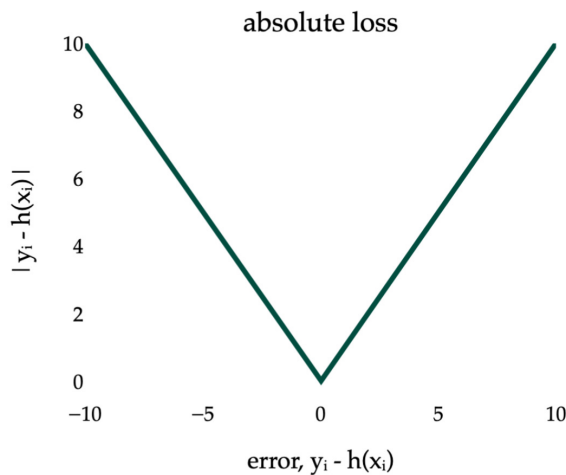
② Choose a loss function

"squared loss"  $L_{sq}(y_i, h(x_i)) = (y_i - h(x_i))^2$

③ Minimize average loss to find optimal parameters

$$R_{sq}(w) = \frac{1}{n} \sum_{i=1}^n (y_i - w)^2 \rightarrow w^* = \text{Mean}(y_1, \dots, y_n) = \bar{y}$$

what if we still use the constant model,  
but use absolute loss instead?

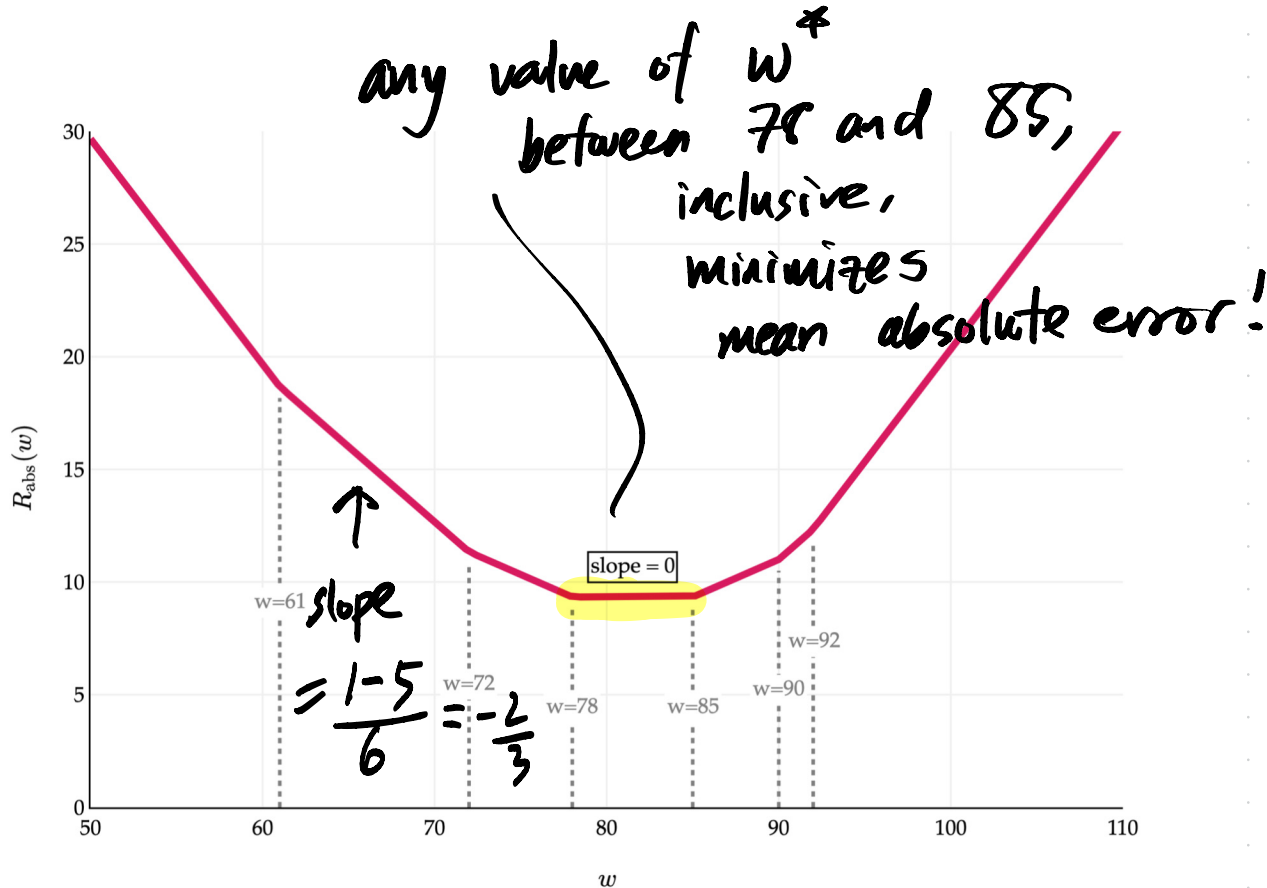


$$R_{\text{abs}}(w) = \frac{1}{5} (|72 - w| + |90 - w| + |61 - w| + |85 - w| + |92 - w|)$$



$$R_{\text{abs}}(w) = \frac{1}{6} (|72 - w| + |90 - w| + |61 - w| + |85 - w| + |92 - w| + |78 - w|)$$

And its graph is:



slope  
at  $w$

$$= \frac{(\# \text{ left of } w) - (\# \text{ right of } w)}{n}$$